

姓名: SOLUTION

葉均承 應數一線性代數

學號: _____

Quiz 10

考試日期: 2021/05/20

1. 請框出答案. 2. 不可使用手機、計算器, 禁止作弊!

1. Express z/w in the form $a + bi$, where $a, b \in \mathbb{R}$, if

$$z = 2 + 3i, w = 5 - i$$

Answer: $z/w = \underline{\underline{\frac{7+17i}{26}}}$

$$1/w = \frac{\bar{w}}{|w|^2} = \frac{5+i}{25+1}$$

$$z/w = \frac{(2+3i)(5+i)}{25+1} = \frac{7+17i}{26}$$

2. Find the six sixth roots of $64i$.

$$64i = 2^6(\cos(\frac{\pi}{2}) + i \sin(\frac{\pi}{2}))$$

$$w_k = 2\left(\cos\left(\frac{\pi}{12} + \frac{2k\pi}{6}\right) + i \sin\left(\frac{\pi}{12} + \frac{2k\pi}{6}\right)\right)$$