

姓名: _____

葉均承

應數一線性代數

學號: _____

Quiz 3

考試日期: 2024/10/02

1. 請框出答案. 2. 不可使用手機、計算器，禁止作弊!

1. Prove that the given relation holds for all real matrices A and B if the expression is defined.

$$(AB)^T = B^T A^T$$

2. Determine whether the vector \vec{b} is in the span of the vectors \vec{v}_i . If so, write \vec{b} into the linear combination form.

p.s. Please solve the problem with the corresponding augmented matrix. Also mark the row-echlon form and reduced row-echlon form of the augmented matrix.

Answer: $\vec{b} = \underline{\hspace{2cm}} \cdot \vec{v}_1 + \underline{\hspace{2cm}} \cdot \vec{v}_2 + \underline{\hspace{2cm}} \cdot \vec{v}_3$

$$\vec{b} = \begin{bmatrix} 3 \\ 0 \\ 3 \end{bmatrix}, \vec{v}_1 = \begin{bmatrix} 0 \\ -1 \\ 1 \end{bmatrix}, \vec{v}_2 = \begin{bmatrix} 2 \\ 1 \\ 1 \end{bmatrix}, \vec{v}_3 = \begin{bmatrix} -1 \\ 2 \\ -3 \end{bmatrix}$$