葉均承 Jean Yeh

Section 3.4

34. T F T T F T F F F T

43.

$$(T_1 + T_2)(\vec{u} + \vec{v}) = T_1(\vec{u} + \vec{v}) + T_2(\vec{u} + \vec{v})$$

= $T_1(\vec{u}) + T_1(\vec{v}) + T_2(\vec{u}) + T_2(\vec{v})$
= $T_1(\vec{u}) + T_2(\vec{u}) + T_1(\vec{v}) + T_2(\vec{v})$
= $(T_1 + T_2)(\vec{u}) + (T_1 + T_2)(\vec{v})$

Similarly,

$$(T_1 + T_2)(r\vec{v}) = T_1(r\vec{v}) + T_2(r\vec{v})$$

= $rT_1(\vec{v}) + rT_2(\vec{v})$
= $r(T_1(\vec{v}) + T_2(\vec{v}))$
= $r(T_1 + T_2)(\vec{v})$

Thus $T_1 + T_2$ is a linear transformation.